

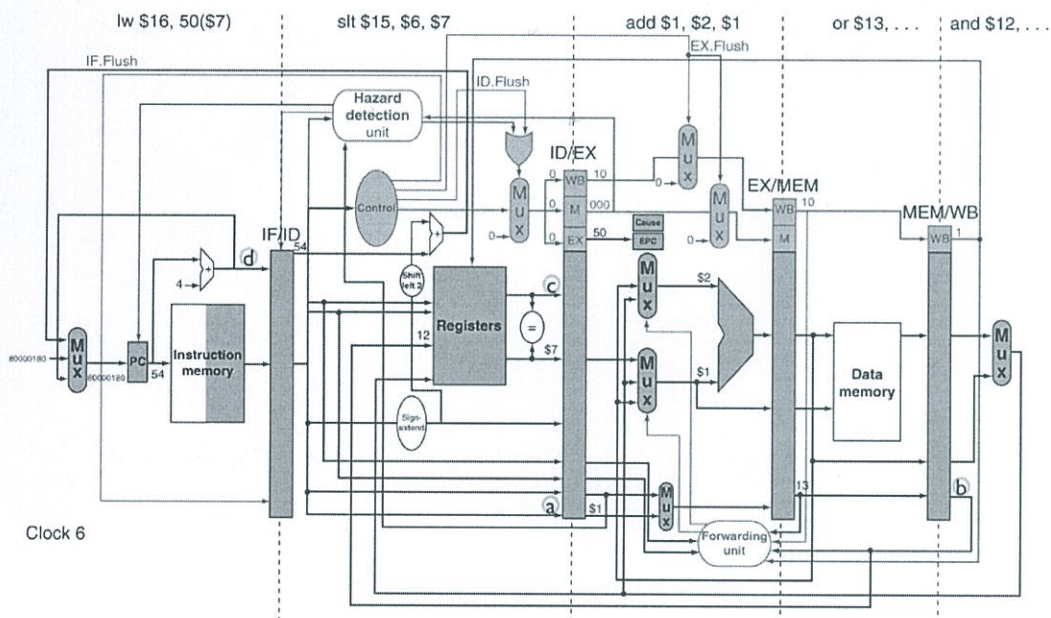
Department of Computer Science, National Tsing Hua University
Ph.D. Qualification Examination
Computer Architecture, Fall 2016

1. (11%) Consider two different implementations M1 and M2 of the same instruction set. M1 has a clock frequency of 1GHz. M2's clock cycle is 1.5ns. There are three classes of instructions with the following CPIs.

Class	CPI for M1	CPI for M2
A	2	2
B	2	1
C	4	3

- (a) (5%) If the number of instructions executed in a certain program is divided equally among the three classes, which machine is faster and by what factor?
- (b) (6%) We can re-design M1 such that the CPI for class-C instructions improves from 4 to 3 (class-A and class-B CPIs remain unchanged). This change, however, would reduce the clock frequency from 1GHz to 900MHz. What should the minimum percentage of class-C instructions be in an instruction mix for this design to result in improved performance?
2. (11%)
- (a) (5%) Explain how the PC-relative addressing mode works.
- (b) (6%) The following instruction allows branching to L1 on register \$s0 being equal to \$s1.
- `beq $s0, $s1, L1`
- Give a pair of instructions that may replace the above instruction and allows location L1 to be much farther away than allowed by the above instruction.
3. (11%)
- (a) (5%) A NAND instruction for performing bitwise NAND of two register values and storing the result into a third register would be nice to have, but why a NAND instruction and many other useful instructions are not included in the MIPS instruction set?
- (b) (6%) Find the shortest sequence of MIPS instructions that will accomplish the same thing as a NAND instruction.

4. (10%) Assume an 8-bit floating point representation with 4-bits exponent and 3-bit fraction besides the one sign bit. The placement of bits is [sign][exponent][fraction] and the bias is 7 (0111_2).
- (a) (5%) Show the floating point 8-bit representation of "-4.5" in binary format.
- (b) (5%) What number is represented by the following single-precision float " 00111001_2 " ?
5. (15%) Compute the number of cycles required to finish the following instructions on the five-stage pipelined MIPS CPU presented in the textbook, assuming that the pipeline initially has NOPs in all stages
- (a) (5%) If there is no forwarding: _____
- (b) (5%) If have EX/MEM and MEM/WB forwarding paths: _____
- (c) (5%) If implement only EX/MEM forwarding path: _____
- lw \$t0, 0(\$s0)
sw \$t0, 4(\$s0)
add \$s0, \$t0, \$t1
sub \$t2, \$s0, \$t3
or \$t2, \$t2, \$s0
6. (8%) What should be the values of a _____, b _____, c _____, d _____



7. (5%) With 32-bit addresses, how many total bits are required for a direct-mapped cache with 32 KB of data and 4-word blocks?
8. (5%) Consider a 7,200 RPM disk with: (i) the average seek time of 3 ms, (ii) the transfer rate of 30 MB/sec, and (iii) the controller overhead of 1ms. What is the average time to write a 512-byte sector, assuming the disk is idle and we are the only user?
9. (6%) For two processors that access on two words $X[0]$ and $X[1]$ of a cache block X following the below operations:

P1: $X[0]=2$; $X[1]--$;
 P2: $X[0]++$, $X[1]=3$;

 - (a) With a correct cache coherence protocol implemented, list all the possible values of $\{(X[0], X[1])\}$.
 - (b) What are the best- and worst-case numbers of cache misses, after finishing all the operations?
10. (6%) Consider a virtual memory system with 64-bit virtual addresses, 16-GB physical RAM, 4-KB page size, and 8-byte Page Table Entry (PTE) size, please answer the following questions:
 - (a) How much physical memory is needed to store the page table if a single-level page table is adopted?
 - (b) With multilevel page tables, we can reduce the physical memory consumption, because only active PTEs are kept in physical memory. How many levels of page tables will be needed in this case?
11. (6%) We bought two disks from manufactures W and S, respectively. The disk from W has a data transfer rate of 10 KB per second and access delay of 5 seconds, while the disk from S has a data transfer rate of 3 KB per second and access delay of 4 seconds.
 - (a) If we receive a request of reading a 5 MB file that is available on both disk, which disk should we read from for the maximum performance?
 - (b) If we receive a request of writing a 10 KB file, which disk should we write the file to, in order to maximize the performance?
12. (6%) Communicating with I/O peripherals can be done by: (i) polling, (ii) interrupt, (iii) memory mapping, and (iv) special I/O commands.
 - (a) (4%) Describe how each of these four approaches works.
 - (b) (2%) Give two sample I/O peripherals that are most suitable for polling and interrupt, respectively, and explain why.

Appendix: MIPS Instruction Reference Sheet

OPCODES, BASE CONVERSION, ASCII SYMBOLS									
MIPS opcode (31:26)	(1) MIPS funct (5:0)	(2) MIPS funct (5:0)	Binary	Deci- mal	Hexa- decim- al	ASCII Char- acter	Deci- mal	Hexa- decim- al	ASCII Char- acter
(1)	sll	add.f	00 0000	0	0	NUL	64	40	@
		sub.f	00 0001	1	1	SOH	65	41	A
j	srl	mul.f	00 0010	2	2	STX	66	42	B
jal	sra	div.f	00 0011	3	3	ETX	67	43	C
beq	sliv	sqr.f	00 0100	4	4	EOT	68	44	D
bne		abs.f	00 0101	5	5	ENQ	69	45	E
blez	srlv		00 0110	6	6	ACK	70	46	F
bgtz	sra	neg.f	00 0111	7	7	BEL	71	47	G
addi	jr		00 1000	8	8	BS	72	48	H
addiu	jalr		00 1001	9	9	HT	73	49	I
slli	movz		00 1010	10	a	LF	74	4a	J
slliu	movn		00 1011	11	b	VT	75	4b	K
andi	syscall	round.w.f	00 1100	12	c	FF	76	4c	L
ori	break	trunc.w.f	00 1101	13	d	CR	77	4d	M
xori		ceil.w.f	00 1110	14	e	SO	78	4e	N
lui	sync	floor.w.f	00 1111	15	f	SI	79	4f	O
(2)	mflhi		01 0000	16	10	DLE	80	50	P
	mthi		01 0001	17	11	DC1	81	51	Q
	mfllo	movz.f	01 0010	18	12	DC2	82	52	R
	mtlo	movn.f	01 0011	19	13	DC3	83	53	S
			01 0100	20	14	DC4	84	54	T
			01 0101	21	15	NAK	85	55	U
			01 0110	22	16	SYN	86	56	V
			01 0111	23	17	ETB	87	57	W
	mult		01 1000	24	18	CAN	88	58	X
	multu		01 1001	25	19	EM	89	59	Y
	div		01 1010	26	1a	SUB	90	5a	Z
	divu		01 1011	27	1b	ESC	91	5b	[
			01 1100	28	1c	FS	92	5c	\
			01 1101	29	1d	GS	93	5d]
			01 1110	30	1e	RS	94	5e	^
			01 1111	31	1f	US	95	5f	_
lb	add	cvt.s.f	10 0000	32	20	Space	96	60	`
lh	addu	cvt.d.f	10 0001	33	21	!	97	61	a
lwl	sub		10 0010	34	22	"	98	62	b
lwr	subu		10 0011	35	23	#	99	63	c
lbu	and	cvt.w.f	10 0100	36	24	\$	100	64	d
lhu	or		10 0101	37	25	%	101	65	e
lwr	xor		10 0110	38	26	&	102	66	f
	nor		10 0111	39	27	'	103	67	g
sb			10 1000	40	28	(104	68	h
sh			10 1001	41	29)	105	69	i
swl	sllt		10 1010	42	2a	*	106	6a	j
sw	slltu		10 1011	43	2b	+	107	6b	k
			10 1100	44	2c	,	108	6c	l
			10 1101	45	2d	-	109	6d	m
swr			10 1110	46	2e	.	110	6e	n
cache			10 1111	47	2f	/	111	6f	o
ll	tge	c.f.f	11 0000	48	30	0	112	70	p
lwl	tgeu	c.un.f	11 0001	49	31	1	113	71	q
lwc2	tlit	c.eq.f	11 0010	50	32	2	114	72	r
pref	tltu	c.ueq.f	11 0011	51	33	3	115	73	s
	teq	c.oit.f	11 0100	52	34	4	116	74	t
ldc1		c.ult.f	11 0101	53	35	5	117	75	u
ldc2	tne	c.oie.f	11 0110	54	36	6	118	76	v
		c.ule.f	11 0111	55	37	7	119	77	w
sc		c.sf.f	11 1000	56	38	8	120	78	x
swc1		c.ngle.f	11 1001	57	39	9	121	79	y
swc2		c.seq.f	11 1010	58	3a	:	122	7a	z
		c.ngl.f	11 1011	59	3b	;	123	7b	{
		c.lt.f	11 1100	60	3c	<	124	7c	
sdcl		c.ngse.f	11 1101	61	3d	=	125	7d	}
sdcl		c.le.f	11 1110	62	3e	>	126	7e	~
		c.ngt.f	11 1111	63	3f	?	127	7f	DEL

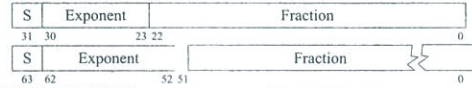
(1) opcode(31:26) == 0
 (2) opcode(31:26) == 17_{ten} (11_{hex}); if fmt(25:21) == 16_{ten} (10_{hex}) f = s (single);
 if fmt(25:21) == 17_{ten} (11_{hex}) f = d (double)

IEEE 754 FLOATING-POINT STANDARD

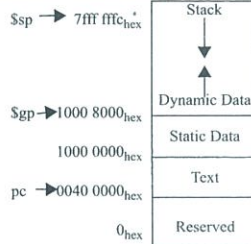
$$(-1)^S \times (1 + \text{Fraction}) \times 2^{(\text{Exponent} - \text{Bias})}$$

where Single Precision Bias = 127.
 Double Precision Bias = 1023.

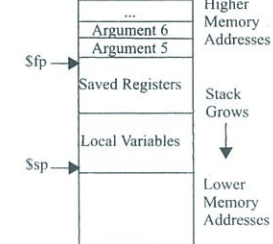
IEEE Single Precision and Double Precision Formats:



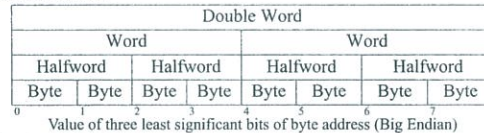
MEMORY ALLOCATION



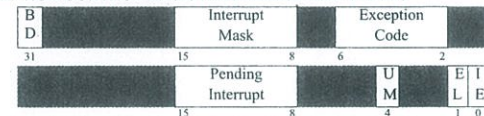
STACK FRAME



DATA ALIGNMENT



EXCEPTION CONTROL REGISTERS: CAUSE AND STATUS



BD = Branch Delay, UM = User Mode, EL = Exception Level, IE = Interrupt Enable

EXCEPTION CODES

Number	Name	Cause of Exception	Number	Name	Cause of Exception
0	Int	Interrupt (hardware)	9	Bp	Breakpoint Exception
4	AdEL	Address Error Exception (load or instruction fetch)	10	RJ	Reserved Instruction Exception
5	AdES	Address Error Exception (store)	11	CpU	Coprocessor Unimplemented
6	IBE	Bus Error on Instruction Fetch	12	Ov	Arithmetic Overflow Exception
7	DBE	Bus Error on Load or Store	13	Tr	Trap
8	Sys	Syscall Exception	15	FPE	Floating Point Exception

SIZE PREFIXES (10^x for Disk, Communication; 2^x for Memory)

SIZE	PRE-FIX	SIZE	PRE-FIX	SIZE	PRE-FIX	SIZE	PRE-FIX
10 ³ , 2 ¹⁰	Kilo-	10 ¹⁵ , 2 ⁵⁰	Peta-	10 ⁻³	milli-	10 ⁻¹⁵	femto-
10 ⁶ , 2 ²⁰	Mega-	10 ¹⁸ , 2 ⁶⁰	Exa-	10 ⁻⁶	micro-	10 ⁻¹⁸	atto-
10 ⁹ , 2 ³⁰	Giga-	10 ²¹ , 2 ⁷⁰	Zetta-	10 ⁻⁹	nano-	10 ⁻²¹	zepto-
10 ¹² , 2 ⁴⁰	Tera-	10 ²⁴ , 2 ⁸⁰	Yotta-	10 ⁻¹²	pico-	10 ⁻²⁴	yocto-

The symbol for each prefix is just its first letter, except μ is used for micro.

MIPS Reference Data

①



CORE INSTRUCTION SET

NAME, MNEMONIC	FOR-MAT	OPERATION (in Verilog)	OPCODE / FUNCT (Hex)
Add	add R	$R[rd] = R[rs] + R[rt]$	(1) 0 / 20 _{hex}
Add Immediate	addi I	$R[rt] = R[rs] + \text{SignExtImm}$	(1,2) 8 _{hex}
Add Imm. Unsigned	addiu I	$R[rt] = R[rs] + \text{SignExtImm}$	(2) 9 _{hex}
Add Unsigned	addu R	$R[rd] = R[rs] + R[rt]$	0 / 21 _{hex}
And	and R	$R[rd] = R[rs] \& R[rt]$	0 / 24 _{hex}
And Immediate	andi I	$R[rt] = R[rs] \& \text{ZeroExtImm}$	(3) c _{hex}
Branch On Equal	beq I	$\text{if}(R[rs] == R[rt])$ $PC = PC + 4 + \text{BranchAddr}$	(4) 4 _{hex}
Branch On Not Equal	bne I	$\text{if}(R[rs] != R[rt])$ $PC = PC + 4 + \text{BranchAddr}$	(4) 5 _{hex}
Jump	j J	$PC = \text{JumpAddr}$	(5) 2 _{hex}
Jump And Link	jal J	$R[31] = PC + 8; PC = \text{JumpAddr}$	(5) 3 _{hex}
Jump Register	jr R	$PC = R[rs]$	0 / 08 _{hex}
Load Byte Unsigned	lbu I	$R[rt] = (24'b0, M[R[rs]] + \text{SignExtImm})(7:0)$	(2) 24 _{hex}
Load Halfword Unsigned	lhu I	$R[rt] = (16'b0, M[R[rs]] + \text{SignExtImm})(15:0)$	(2) 25 _{hex}
Load Linked	ll I	$R[rt] = M[R[rs] + \text{SignExtImm}]$	(2,7) 30 _{hex}
Load Upper Imm.	lui I	$R[rt] = \{imm, 16'b0\}$	f _{hex}
Load Word	lw I	$R[rt] = M[R[rs] + \text{SignExtImm}]$	(2) 23 _{hex}
Nor	nor R	$R[rd] = \sim (R[rs] R[rt])$	0 / 27 _{hex}
Or	or R	$R[rd] = R[rs] R[rt]$	0 / 25 _{hex}
Or Immediate	ori I	$R[rt] = R[rs] \text{ZeroExtImm}$	(3) d _{hex}
Set Less Than	slt R	$R[rd] = (R[rs] < R[rt]) ? 1 : 0$	0 / 2a _{hex}
Set Less Than Imm.	slti I	$R[rt] = (R[rs] < \text{SignExtImm}) ? 1 : 0$	(2) a _{hex}
Set Less Than Imm. Unsigned	sltiu I	$R[rt] = (R[rs] < \text{SignExtImm}) ? 1 : 0$	(2,6) b _{hex}
Set Less Than Unsig.	sltu R	$R[rd] = (R[rs] < R[rt]) ? 1 : 0$	(6) 0 / 2b _{hex}
Shift Left Logical	sll R	$R[rd] = R[rs] \ll \text{shamt}$	0 / 00 _{hex}
Shift Right Logical	srl R	$R[rd] = R[rs] \gg \text{shamt}$	0 / 02 _{hex}
Store Byte	sb I	$M[R[rs] + \text{SignExtImm}](7:0) = R[rt](7:0)$	(2) 28 _{hex}
Store Conditional	sc I	$M[R[rs] + \text{SignExtImm}] = R[rt];$ $R[rt] = (\text{atomic}) ? 1 : 0$	(2,7) 38 _{hex}
Store Halfword	sh I	$M[R[rs] + \text{SignExtImm}](15:0) = R[rt](15:0)$	(2) 29 _{hex}
Store Word	sw I	$M[R[rs] + \text{SignExtImm}] = R[rt]$	(2) 2b _{hex}
Subtract	sub R	$R[rd] = R[rs] - R[rt]$	(1) 0 / 22 _{hex}
Subtract Unsigned	subu R	$R[rd] = R[rs] - R[rt]$	0 / 23 _{hex}

- (1) May cause overflow exception
- (2) $\text{SignExtImm} = \{16(\text{immediate}[15]), \text{immediate}\}$
- (3) $\text{ZeroExtImm} = \{16(1b'0), \text{immediate}\}$
- (4) $\text{BranchAddr} = \{14(\text{immediate}[15]), \text{immediate}, 2'b0\}$
- (5) $\text{JumpAddr} = \{PC + 4[31:28], \text{address}, 2'b0\}$
- (6) Operands considered unsigned numbers (vs. 2's comp.)
- (7) Atomic test&set pair; $R[rt] = 1$ if pair atomic, 0 if not atomic

BASIC INSTRUCTION FORMATS

R	opcode	rs	rt	rd	shamt	funct
	31	26 25	21 20	16 15	11 10	6 5
	0					
I	opcode	rs	rt	immediate		
	31	26 25	21 20	16 15		
	0					
J	opcode	address				
	31	26 25				
	0					

ARITHMETIC CORE INSTRUCTION SET

② OPCODE

NAME, MNEMONIC	FOR-MAT	OPERATION	(Hex)
Branch On FP True	bclt FI	$\text{if}(FPcond) PC = PC + 4 + \text{BranchAddr}$	(4) 11/8/1/--
Branch On FP False	bclt FI	$\text{if}(!FPcond) PC = PC + 4 + \text{BranchAddr}$	(4) 11/8/0/--
Divide	div R	$Lo = R[rs] / R[rt]; Hi = R[rs] \% R[rt]$	0/--/--/1a
Divide Unsigned	divu R	$Lo = R[rs] / R[rt]; Hi = R[rs] \% R[rt]$	(6) 0/--/--/1b
FP Add Single	add.s FR	$F[fd] = F[fs] + F[ft]$	11/10/--/0
FP Add Double	add.d FR	$\{F[fd], F[fd+1]\} = \{F[fs], F[fs+1]\} + \{F[ft], F[ft+1]\}$	11/11/--/0
FP Compare Single	c.x.s* FR	$FPcond = (F[fs] op F[ft]) ? 1 : 0$	11/10/--/y
FP Compare Double	c.x.d* FR	$FPcond = (\{F[fs], F[fs+1]\} op \{F[ft], F[ft+1]\}) ? 1 : 0$	11/11/--/y
* (x is eq, lt, or le) (op is ==, <, or <=) (y is 32, 3c, or 3e)			
FP Divide Single	div.s FR	$F[fd] = F[fs] / F[ft]$	11/10/--/3
FP Divide Double	div.d FR	$\{F[fd], F[fd+1]\} = \{F[fs], F[fs+1]\} / \{F[ft], F[ft+1]\}$	11/11/--/3
FP Multiply Single	mul.s FR	$F[fd] = F[fs] * F[ft]$	11/10/--/2
FP Multiply Double	mul.d FR	$\{F[fd], F[fd+1]\} = \{F[fs], F[fs+1]\} * \{F[ft], F[ft+1]\}$	11/11/--/2
FP Subtract Single	sub.s FR	$F[fd] = F[fs] - F[ft]$	11/10/--/1
FP Subtract Double	sub.d FR	$\{F[fd], F[fd+1]\} = \{F[fs], F[fs+1]\} - \{F[ft], F[ft+1]\}$	11/11/--/1
Load FP Single	lwc1 I	$F[rt] = M[R[rs] + \text{SignExtImm}]$	(2) 31/--/--/0
Load FP Double	ldc1 I	$F[rt] = M[R[rs] + \text{SignExtImm}];$ $F[rt+1] = M[R[rs] + \text{SignExtImm} + 4]$	(2) 35/--/--/0
Move From Hi	mghi R	$R[rd] = Hi$	0/--/--/10
Move From Lo	mfl0 R	$R[rd] = Lo$	0/--/--/12
Move From Control	mfc0 R	$R[rd] = CR[rs]$	10/0/--/10
Multiply	mult R	$\{Hi, Lo\} = R[rs] * R[rt]$	0/--/--/18
Multiply Unsigned	multu R	$\{Hi, Lo\} = R[rs] * R[rt]$	(6) 0/--/--/19
Shift Right Arith.	sra R	$R[rd] = R[rt] \gg \text{shamt}$	0/--/--/3
Store FP Single	swc1 I	$M[R[rs] + \text{SignExtImm}] = F[rt]$	(2) 39/--/--/0
Store FP Double	sdc1 I	$M[R[rs] + \text{SignExtImm}] = F[rt];$ $M[R[rs] + \text{SignExtImm} + 4] = F[rt+1]$	(2) 3d/--/--/0

FLOATING-POINT INSTRUCTION FORMATS

FR	opcode	fmt	ft	fs	fd	funct
	31	26 25	21 20	16 15	11 10	6 5
	0					
FI	opcode	fmt	ft	immediate		
	31	26 25	21 20	16 15		
	0					

PSEUDOINSTRUCTION SET

NAME	MNEMONIC	OPERATION
Branch Less Than	b.lt	$\text{if}(R[rs] < R[rt]) PC = \text{Label}$
Branch Greater Than	b.gt	$\text{if}(R[rs] > R[rt]) PC = \text{Label}$
Branch Less Than or Equal	b.le	$\text{if}(R[rs] \leq R[rt]) PC = \text{Label}$
Branch Greater Than or Equal	b.ge	$\text{if}(R[rs] \geq R[rt]) PC = \text{Label}$
Load Immediate	li	$R[rd] = \text{immediate}$
Move	move	$R[rd] = R[rs]$

REGISTER NAME, NUMBER, USE, CALL CONVENTION

NAME	NUMBER	USE	PRESERVED ACROSS A CALL?
\$zero	0	The Constant Value 0	N.A.
\$at	1	Assembler Temporary	No
\$v0-\$v1	2-3	Values for Function Results and Expression Evaluation	No
\$a0-\$a3	4-7	Arguments	No
\$t0-\$t7	8-15	Temporaries	No
\$s0-\$s7	16-23	Saved Temporaries	Yes
\$t8-\$t9	24-25	Temporaries	No
\$k0-\$k1	26-27	Reserved for OS Kernel	No
\$gp	28	Global Pointer	Yes
\$sp	29	Stack Pointer	Yes
\$fp	30	Frame Pointer	Yes
\$ra	31	Return Address	Yes